

The NUTEV DIS $\sin^2\theta_W$ Anomaly

or

Beware of Mass Singularities
($\ln(M/m_f)$ terms)

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Lunch Discussion



Based on: **Oldies but Goodies**

WJM & A. Sirlin (1973) electron-muon universality

WJM (1975) Dim. Reg. of mass singularities

D. Albert, WJM, Z. Parsa, D. Wyler (1980) *W & Z Decays*

*A. Sirlin and WJM (1981) *Neutrino DIS & $\sin^2\theta_w$*

More Recent

A. Czarnecki, WJM, G.P. Lepage (2000) *Muonium Decay*

2020 Nobel Prize Connection

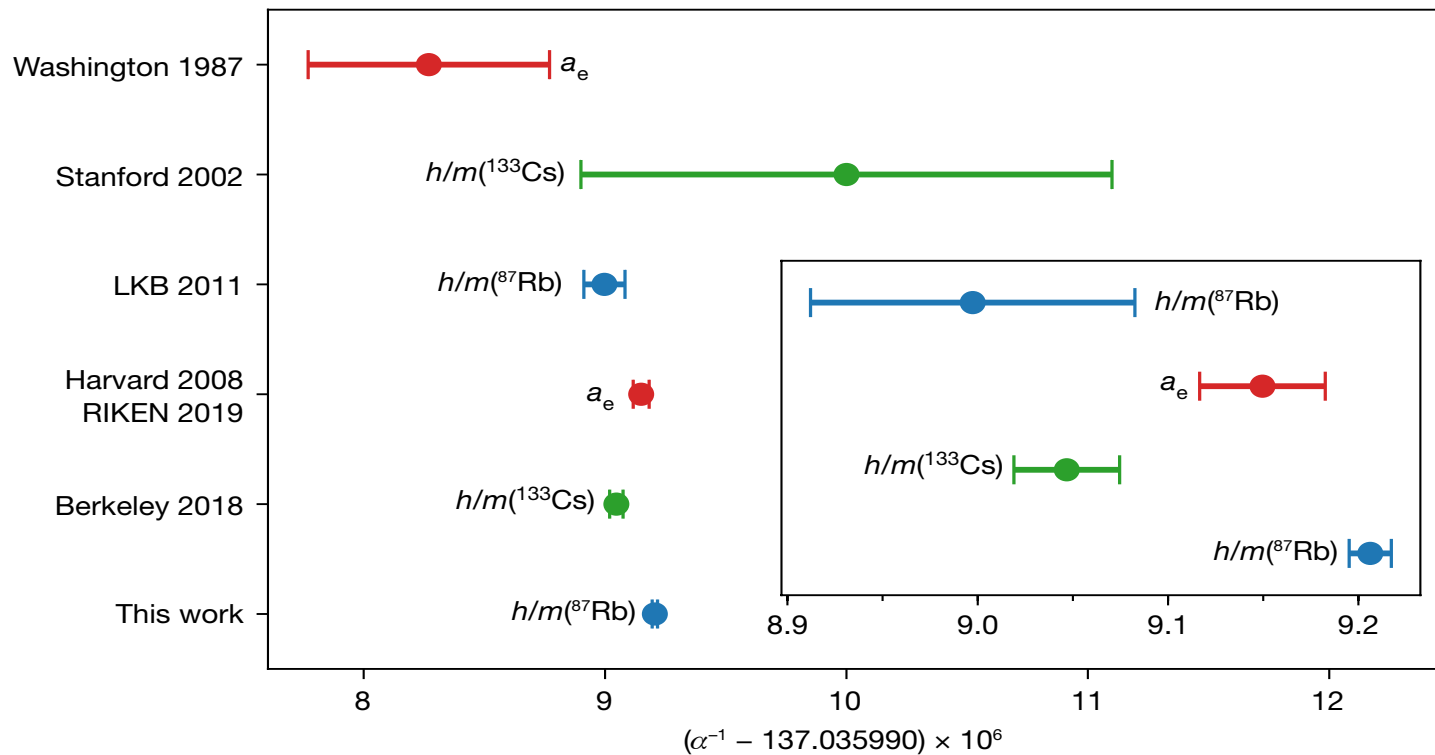
Black Holes and BNL

Precision EW Parameters (status):

<u>Quantity</u>	<u>2008 Value</u>	<u>2020 Value</u>	<u>Comment</u>
α^{-1}	137.035999084(51)	137.035999046(27)	$\alpha^{-1}(\text{Cs})$
		137.035999150(34)	$\alpha^{-1}(a_e)$
		137.035999206(11)	$\alpha^{-1}(\text{Rb})$ 5.5 σ tension New!
G_μ	$1.16637(1) \times 10^{-5} \text{GeV}^{-2}$	1.1663787(6) $\times 10^{-5} \text{GeV}^{-2}$	τ_{μ^+} PSI MuLAN 2010
m_Z	91.1875(21) GeV	91.1876(21) GeV	-
* m_t	171.4(2.1) GeV \rightarrow	172.9(0.4) GeV	FNAL/LHC
* m_H	>114 GeV \rightarrow	125.10(0.14) GeV	LHC
m_W	80.410(32) GeV \rightarrow	80.379(12) GeV	LEP2/FNAL/LHC
		80.359(3) GeV	Global Fit Value
$\sin^2\theta_W(m_Z)$	0.23070(26)	0.23070(26)	SLAC A_{LR}
$\sin^2\theta_W(m_Z)$	0.23193(29)	0.23193(29)	CERN $A_{FB}(bb)$
	(3 sigma difference?)		
$\sin^2\theta_W(m_Z)_{ave}$	0.23125(16)	0.23119(14)	Z Pole Ave.
		0.23120(6)	Global EW Fit

Comparison of recent α determinations from Nature (2020)
 5.5 sigma difference between $\alpha(\text{Rb})$ and $\alpha(\text{Cs})$

$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}}$ changes sign!



Comment on New $\alpha(Rb)$ value

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = -87(28)_{\text{exp}}(23)_{\alpha}(2)_{\text{th}} \times 10^{-14} \quad \text{for Cs}$$

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = +47(28)_{\text{exp}}(9)_{\alpha}(2)_{\text{th}} \times 10^{-14} \quad \text{for Rb sign change}$$

$$\Delta a_{\mu} = a_{\mu}^{\text{exp}} - a_{\mu}^{\text{SM}} = +261(40)(26) \times 10^{-11}$$

$$\frac{\Delta a_{\mu}}{\Delta a_e} \sim 5553 \quad \text{if } m_{\mu}^2/m_e^2 \text{ scaling holds, e}/\mu \text{ universality,}$$
$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} \sim 6 \times 10^{-14} \text{ expected}$$

Accommodate with a light Scalar

But first overcome Rb/Cs Difference

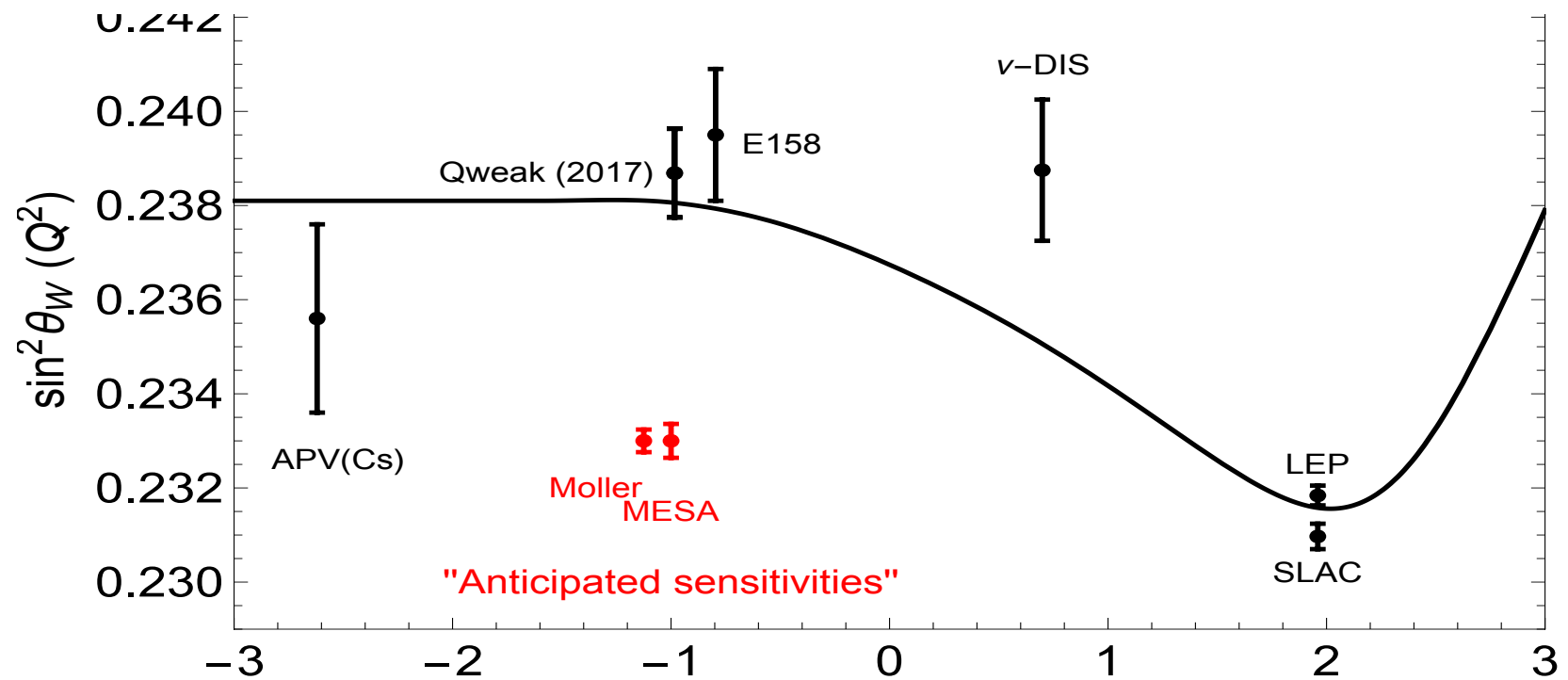
Best Off Z Resonance Measurements of $\sin^2\theta_W(m_Z)_{MS}$
(Not Yet Competitive with Z Pole)

Reaction	$\sin^2\theta_W(m_Z)_{MS}$	$\langle Q \rangle$
Cs APV	0.2283(20)	2.5MeV
E158 ee	0.2329(13)	160MeV
Q_{weak} ep	<u>0.2310(11)</u>	160MeV
Average	0.23127(77)	Good Agreement
Z Pole	0.23119(14)	
*NuTeV $\nu_\mu N$	0.23560(160)	10 GeV

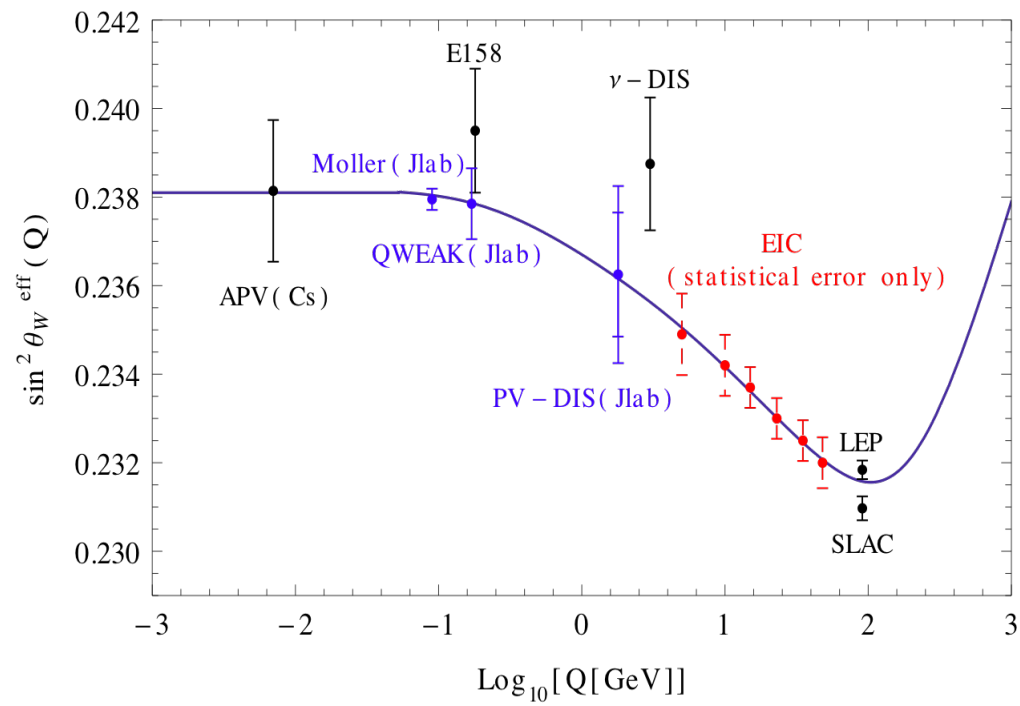
NuTeV high by about 2-3 sigma using $R_\nu^{exp} = \sigma_{NC}/\sigma_{CC} = 0.3916(7)$

BSM Unlikely? R_ν incomplete Radiative Corrections? Likely!

Running of the Weak Mixing Angle



Running of $\sin^2\vartheta_W(Q)$ & Future Measurements



Radiative corrections to R_ν (A. Sirlin & WJM 1981)

$$R_\nu^{exp} \equiv \sigma(\nu_\mu N \rightarrow \nu_\mu X) / \sigma(\nu_\mu N \rightarrow \mu X') = 0.3916(7) \text{ NuTeV.} \quad (2002)$$

Radiative Corrections 1 loop + Bremsstrahlung (Monte Carlo)

$$\text{Experiment: } \sin^2 \theta_W \equiv 1 - \frac{m_W^2}{m_Z^2} = 0.2277(16) \text{ vs SM global fit} \rightarrow \underline{0.2234(1)}$$

Main RC from $W\gamma$ **Box diagram increases** CC cross-section by $\frac{\alpha}{\pi} (\ln \frac{m_Z^2}{2Q^2} + 2) \sim 1.8\%$

Suggests R_ν^{SM} needs additional correction by $\sim 0.9\%$ to agree with Global average

Mass Singularities theorem (1959) No large $O(\frac{\alpha}{2\pi} \ln(\frac{2m_N E_\nu}{m_\mu^2})) \sim 1\%$

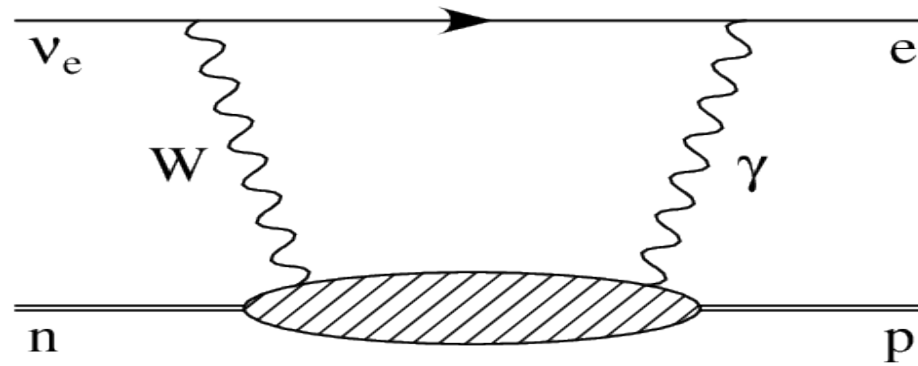
corrections for $\nu_\mu N \rightarrow \mu X'$ fully inclusive cross-section over all E_μ .

However, cuts on Bremsstrahlung induce mass singularities. Increase CC cross-section by about $+0.8\text{-}0.9\%$. Just what is needed for agreement with SM. **Already included??**

Predicted by A. Sirlin & WJM in 1981! **Generic +0.7%**

Recently gifted to NuTeV Collaboration for consideration. The Jury is still out.

Box Diagram Loop Induced RC



Example of cuts: e/μ Universality Breakdown in $W \rightarrow l\nu(\gamma)$ decays ($l=e,\mu$)

Dimensional Regularization of both infrared div. & lepton mass sing. $m_\gamma=0$ $m_l=0$
 Compare with $m_l \neq 0$ calculation, neglecting $O(\frac{m_l^2}{m_W^2})$ effects taking $n \rightarrow 4$

$$\text{Inclusive Decay Rate} = g^2 \frac{m_W}{48\pi} \left(1 - \frac{\alpha}{2\pi} \left(\frac{2\pi}{3} - \frac{77}{12}\right)\right) \rightarrow \frac{\Gamma(W \rightarrow e\nu(\gamma))}{\Gamma(W \rightarrow \mu\nu(\gamma))} = 1 + O\left(\frac{m_l^2}{m_W^2}\right)$$

$$\text{Exclusive } E_{\max} - \Delta E \leq E \leq E_{\max} \frac{\Gamma(W \rightarrow e\nu(\gamma), \Delta E)}{\Gamma(W \rightarrow \mu\nu(\gamma), \Delta E)} = 1 - \frac{\alpha}{2\pi} \left[\left(4 \ln \frac{m_W}{2\Delta E} - 3\right) \ln \frac{m_\mu}{m_e} \right]$$

$$\text{Exponentiate} = \left(\frac{2\Delta E}{m_W}\right)^{0.0248} (1.018)$$

Cuts can affect Universality tests

$$= \underline{0.93 \text{ for } \Delta E = 1\text{GeV}}$$

eg. $B \rightarrow Kl^+ l^-$ **New Physics? EXP?**

e/μ detection differences

Precision Muon (μ^+) Lifetime $\rightarrow GF$

MuLAN experiment at PSI:

$$\tau_{\mu^+} = 2.1969803(22) \times 10^{-6} \text{sec} \quad \text{MuLAN 2010}$$

(Most precise lifetime measurement ever!)

Lowered Previous World Average error by 1/20!

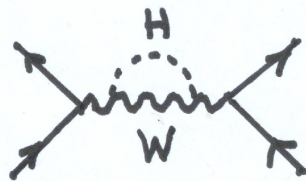
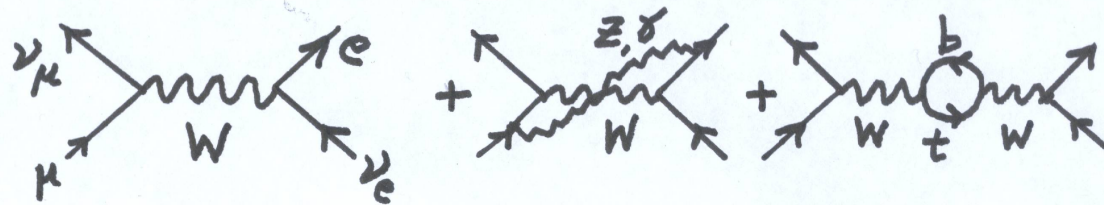
$$\tau_{\mu}^{-1} = \Gamma(\mu^+ \rightarrow e^+ \nu_e \nu_{\mu}(\gamma)) = G_{\mu}^2 m_{\mu}^5 f(m_e^2/m_{\mu}^2) [1 + \text{RC}] / 192 \pi^3$$

$$\text{RC} = \alpha / 2\pi (25/4 - \pi^2) (1 + \alpha / \pi [2/3 \ln(m_{\mu}/m_e) - 3.7] \dots) \quad \text{Fermi Th.}$$

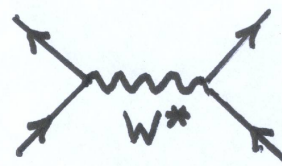
Other SM and “New Physics” radiative corrections absorbed into G_{μ} . Eg. 4th generation, Technicolor, W^* ...

$$G_F \equiv G_{\mu} = 1.1663787(6) \times 10^{-5} \text{GeV}^{-2} \quad \text{precise \& important normalization}$$

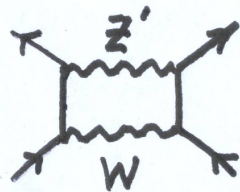
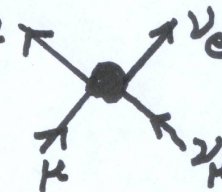
Loop and Tree Level Corrections to Muon Decay



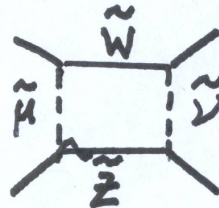
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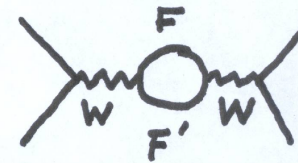
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Z' Boson

SUSY

Technicolor

+ ...

Lessons Learned From Muonium
in Vernon Hughes Memorial Symposium 2003
based on Czarnecki, Lepage & Marciano PRD61 (2000)

MuLan μ^+ Lifetime 1ppm measurement of $\tau_\mu \rightarrow G_\mu \rightarrow G_{\text{Fermi}}$

Stopped μ^+ in matter forms muonium $M=\mu^+e^-$ state

Phase space reduction cancels Final State Interaction!

Spectrum Changes $O(\alpha^2 m_e/m_\mu)$ from each

Cancel due to Lorentz & Gauge Invariance

Bound State Ward Identity

$\tau_M = \tau_\mu(1 + \frac{1}{2}\alpha^2 m_e^2/m_\mu^2 + \text{higher order})$

leading correction time dilation $\approx O(10^{-9})$

Muon lifetime G_μ should not be source of V_{ud} unitarity Problem

$V_{ud}=0.97370(14)$: $|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 0.9985(5)$ 3 sigma tension

Phase Space Suppression cancels FSI e^+e^- (many examples)

Similar to Cancellation of Mass Singularities: Kinoshita & Sirlin (1959)

- Muonium $\pm 5\alpha^2 m_e/m_\mu$ linear contributions cancel
- General bound state theorem based on gauge invariance (QED and QCD)
- 1952 [The Effect of Atomic Binding on Nuclear Reaction Energies](#) Nuclear Beta Decay [Serber & Snyder](#) (first use of theorem)
- 1960 Muon capture [Uberall](#) (important potentially large effect)
- Bottom Decays (lifetimes) OPE Proof no $1/m_b$ effects
- **Superaligned Nuclear Beta Decays – Complicated at 0.1%**
Possible $O(Z^{4/3}\alpha^2 m_e/M)$ source of discrepancy?

[Future Work](#)

Inventors of Strong Focusing at BNL



Courant

Livingston

Snyder

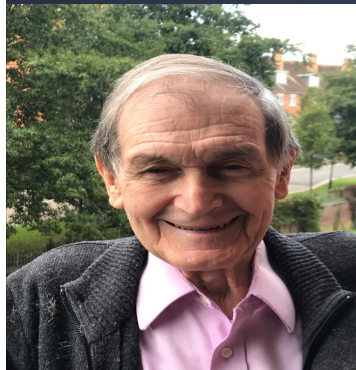
The Legacy Of Hartland Sweet Snyder
(A Human Interest Story)

“The Effect of Atomic Binding on Nuclear Reaction Energies”
by R. Serber and H.S. Snyder PR87(1952). **10 citations** (I was last in 2004))

“The strong-focusing synchrotron: A new high-energy accelerator”
by Courant, Livingston & Snyder PR88(1952). **135 Citations**

“Quantized space-time” H.S. Snyder PR71(1947)
1751 citations (100 in 2019!)

“On continued gravitation contraction” PR56(1939)
by J. Oppenheimer and H. Snyder (***Classical Black Holes Exist!***) **876 citations**



Roger Penrose



Hartland "sweet" Snyder



Robert Oppenheimer

2020 Physics Nobel Prize to Roger Penrose for Black Hole stability. Motivated by the early work of Snyder and Oppenheimer (1939) (Ahead of its Time)

Maurice Goldhaber and Ernest Courant BNL Centenarians

